

Thermodynamics and Statistical Mechanics—Content(64 hours)

(SJTU Zhiyuan College Physics Major Undergraduate)

Part one: Framework of equilibrium stat. mech. (26-28 hours)

Chapter 1 Thermodynamics (4-5 hours)

- 1) Large systems, small systems, macroscopic states and microscopic states, thermodynamic equilibrium
 - 2) Zeroth laws of thermodynamics, equivalence class, definition of temperature
 - 3) First law, conservation of energy, heat, work, conjugate variables, perpetual motion of first kind
 - 4) Second law, heat engine, Carnot theorem, Entropy, Principle of maximum entropy,
 - 5) Arrow of time, paradox of irreversibility, perpetual motion, absolute temperature
 - 6) Third law and its quantum mechanical origin
- Selective topic: Cooling techniques, history and status quo

Chapter 2 Ensemble theory (10-12 hours)

- 1) Microcanonical ensemble, isolated systems, fundamental postulate of equal a priori probability, Boltzmann Entropy, principle of maximum entropy
- 2) Conditions of equilibrium, condition of stability, temperature, pressure, chemical potential
- 3) Canonical ensemble, Gibbs distribution, partition function, Helmholtz free energy, thermodynamic relations, fluctuations, central limit theorem, equivalence of ensembles
- 4) Grand canonical ensemble, grand potential, Gibbs Duhem relation
- 5) Principle of maximal entropy revisited, principle of minimal free energy, and equivalence with the fundamental postulate, Lagrange multiplier.

Selective topic: Variational principle in theoretical physics

Chapter 3 Description and evolution of many body states (10-12 hours)

Quantum systems (6-8 hours)

- 1) Manybody states, mixed state, density matrix
- 2) Evolution of density matrix, Von Neumann entropy, Von Neumann equation, evolution of entropy, quantum entanglement
- 3) Quantum ensembles, theorem of spin-statistics, Pauli's exclusion principle, Slater determinant
- 4) Fermi-Dirac statistics, Bose-Einstein statistics,
- 5) High temperature limit, Maxwell-Boltzmann statistics

Classical systems (4 hours)

- 1) Hamiltonian equation, Liouville equation, Poisson Bracket
- 2) Liouville theorem, Gibbs entropy and its evolution
- 3) Poincare's recurrence theorem, ergodicity, mixing, chaos

Selective topics: Entropy, information entropy, quantum entanglement entropy

Part two: Applications of equilibrium statistical mechanics (26 hours)

Chapter 4 Non-interacting systems (12 hours)

Classical systems (3-4 hours):

- 1) Ideal gas, gas mixture, Gibbs paradox, Maxwell's demon, mixing entropy
- 2) Equipartition and its failure, poly-atomic molecular gas.
- 3) Two level systems, negative temperature,
- 4) paramagnetism, Curie's law, Ising model

Quantum systems (8-10 hours):

- 1) Density of states, one, two, three dimensional cases, boundary conditions
- 2) Fermi gas, Sommerfeld expansion, high T expansion, low T expansion
- 3) White dwarf, neutron star, black hole
- 4) Bose gas, BEC, Debye theory for lattice vibration,
- 5) Black body radiation, Johnson noise, cosmic microwave background
- 6) Bose-Einstein condensation

Chapter 5 Interacting many body systems (6 hours)

- 1) Interacting gas, Mayer's cluster expansion, van der Waals equation
- 2) Hard sphere gas, Onsager's theory for nematic liquid crystals
- 3) Coulomb gas, Poisson-Boltzmann theory, Debye Hucke theory

Chapter 6 Phase transitions (6-8 hours)

- 1) Classification of phase transition, phase diagram, Ising model, Mean field theory
- 2) 2nd order phase transition, Landau theory, order parameter, symmetry breaking
- 3) Critical phenomena, scaling law, renormalization group, soft modes, fluctuations, topological defects
- 4) 1st order phase transition, coexistence, domain wall, binary systems, phase separation

Selective: topics: Spinodal decomposition, generalized elasticity, quantum phase transitions

Part Three: Non-equilibrium statistical mechanics (8 hours)

Chapter 7 Non-equilibrium Phenomena (4-6 hours)

- 1) Linear response theory
- 2) Fluctuation-dissipation theorem, Onsager's reciprocal relations
- 3) Brownian motions, Langevin equation

Selective topics: Fluctuation theorem, Jarzynski equality

Chapter 8 Paradox of irreversibility revisited (2 hours)

Selective: topics: Irreversibility of classical systems, ergodicity, recurrence, chaos

Selective: topics: Irreversibility of quantum systems, measurement, collapse of wave functions, many universe, decoherence,

Selective: topics: Second law, arrow of time

Review and Summary (2 hours)

Student Presentation (2-4 hours)

Topics of Essays:

- 1) Cooling techniques, history and status quo
- 2) Variational principle in theoretical physics
- 3) Thermodynamic entropy, Gibbs entropy, information entropy, and quantum entanglement entropy
- 4) Poincare's recurrence theorem, ergodicity, chaos, arrow of time, second law
- 5) Quantum mechanical irreversibility, collapse of wave function, multi-universe, decoherence
- 6) Cosmic microwave background, big bang, origin and destiny of universe
- 7) Phase transition, symmetry breaking, Ising model, critical phenomena
- 8) Symmetry breaking and generalized elasticity
- 9) Liouville theorem and Jarzynski equality, fluctuation theorems
- 10) Random walk and statistics of polymers
- 11) Any other interesting topics related to statistical physics (need consensus from the instructor)